# **PyTuning Documentation**

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PyTuning is a Python library intended for the exploration of musical scales and microtonalities. It can be used by developers who need ways of calculating, analyzing, and manipulating musical scales, but it can also be used interactively.

It makes heavy use of the SymPy package, a pure-Python computer algebra system, which allows scales and scale degrees to be manipulated symbolically, with no loss of precision. There is also an optional dependency on Matplotlib (and Seaborn) for some visualizations that have been included in the package.

Some of the package's features include:

- Creation of scales in a variety of ways (EDO, Euler-Fokker, Diatonic, Harmonic, from generator intervals, etc.)
- Ability to represent created scales in ways that are understood by external software (Scala, Timidity, Fluidsynth, Yoshimi, Zvnaddsubfx).
- Some analysis functions (for example, PyTuning provides a framework for searching for scale modes based upon defined metric functions and combinatorial analysis). Also included are some number-theoretic functions, such as prime limits and odd limits.
- · Some scale visualizations.
- · Interactive use.

As a simple example, to create a 31-TET scale and then create a tuning table for the timidity soft-synth:

```
scale = create_edo_scale(31)
tuning_table = create_timidity_tuning(scale, reference_note=69)
```

The design of PyTuning is purposefully simple so that non-computer professionals can use it without much difficultly (musicians, musicologist, interested people of all stripes).

In scope this project is similar to the Scala software package, with a few differences:

- Scala is a mature, full-featured package that includes many, many scales and functions for manipulating and analyzing those scales. This project is much newer and less mature; its scope is currently much less (but hopefully it will be easy to extend).
- PyTuning is written in Python and relies on modern, well maintained dependencies. Scala is written in Ada, and while this is an interesting choice, it probably limits the population of users who *could* change or extend it should a need arise.
- Scala is mainly an application. PyTuning is a development library, but with ways for non-programmers to use it interactively.
- This package does *not* interact with sound cards or audio drivers, so one can't play a scale directly. There are, however, functions for exporting scales into other software packages so that music and sound can be produced.

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# Installation

PyTuning runs under Python 2.7.X and 3.X.

The easiest way to install PyTuning is via the Python Package Index, with which Pytuning is registered:

pip install pytuning

There are two hard dependencies for PyTuning: SymPy and NumPy. SymPy is a pure Python library and pip will handle its installation nicely. NumPy is a more complicated package and if installed via pip may involve much compilation; it would probably behoove you to install the package manually via whatever mechanism your platform provides before pip installing the package.

If you are running the package interactively it is recommended that the Jupyter interactive shell be installed. This is discussed in the documentation under the notes on Interactive use.

The source-code is available on GitHub, where it can be cloned and installed.

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# **Documentation**

Documentation for the package can be found on Read the Docs.

# Roadmap

More scales, more visualizations, more analysis functions. Pull requests are welcome!

# 3.1 Basic Concepts

PyTuning is purposefully designed to be as simple as possible, so that non-programmers (musicologists, musicians, etc.) can use it without too much difficulty: the data structures are relatively simple; there are currently no classes defined, instead opting for an imperative/procedural approach.

Regardless of how it is used (interactively or as a development library), the user should have a good understanding of some of the basic, foundational concepts the package uses.

#### **3.1.1 Scales**

A **scale** is, simply, a list of degrees. By convention the list is bookended by the unison and the octave, with each degree given as a frequency ratio relative to the root tone of the scale. The first degree is always 1, the ratio of the first degree to the first degree. Most commonly the last degree is 2, as the octave is usually twice the frequency of the root (although the package has some support for non-standard "octaves").

As an example, this is the standard 12-tone equal temperament scale (sometimes referred to as 12-TET, or 12-EDO, for Equal Division of the Octave).

$$\left[1,\quad \sqrt[12]{2},\quad \sqrt[6]{2},\quad \sqrt[4]{2},\quad \sqrt[3]{2},\quad 2^{\frac{5}{12}},\quad \sqrt{2},\quad 2^{\frac{7}{12}},\quad 2^{\frac{2}{3}},\quad 2^{\frac{3}{4}},\quad 2^{\frac{5}{6}},\quad 2^{\frac{11}{12}},\quad 2\right]$$

A few things to note:

- As mentioned previously, the scale includes the unison and octave.
- Each scale degree is a SymPy number, so it is represented symbolically. Note that algebraic simplifications are performed by default.
- Even though the length of this list of 13, it is considered a 12 note scale, because the unison and the octave is in actuality the same note. Many of the functions in this package ask one to choose the number of notes or degrees to be used in this function. For these you should follow this convention.

(For those who are curious: the generation of scales is documented in *Scale Creation*, but the above scale was generated with the following code:

```
from pytuning.scales import create_edo_scale
edo_12_scale = create_edo_scale(12)
```

Simplified versions of most functions are provided in the interactive environment.)

## 3.1.2 Degrees

Scale degrees (which are expressed as frequency rations relative to the tonic of the scale) are expressed in SymPy values. In practical terms the Integer and Rational class will be used the most, but SymPy is a full-featured package, and you may benefit from having some familiarity with it.

An example of a few degrees:

Will yield the following:

 $\begin{array}{c}
1 \\
2 \\
\frac{3}{2} \\
\sqrt[12]{2} \\
2^{\frac{1}{2\pi}}
\end{array}$ 

SymPy manipulates all values analytically, but sometimes one needs a floating approximation to a degree (for example, tuning a synthesizer usually needs frequencies expressed as floating point numbers). For the <code>evalf()</code> member function can be used:

```
print(unison.evalf())
1.0000000000000
print(octave.evalf())
2.00000000000000
print(perfect_fifth.evalf())
1.50000000000000
print(minor_second_tet.evalf())
1.05946309435930
print(lucy_L.evalf())
1.11663288009114
```

#### **3.1.3 Modes**

A **mode** is a selection of notes from a scale, and is itself a list of degrees (and therefore is also a scale). A mode can be produced from a scale by applying a **mask** to the scale. Again, the functions involved are documented elsewhere, but as example this is how we would produce the standard major scale (which in the context of this package would be referred to as a mode):

```
major_mask = (0,2,4,5,7,9,11,12)
major_mode = mask_scale(edo_12_scale, major_mask)
```

which produces the following scale:

$$\left[1,\quad \sqrt[6]{2},\quad \sqrt[3]{2},\quad 2^{\frac{5}{12}},\quad 2^{\frac{7}{12}},\quad 2^{\frac{3}{4}},\quad 2^{\frac{11}{12}},\quad 2\right]$$

# 3.1.4 Mode Objects

Some functions in this package return a **mode object**. For example, the find\_best\_modes() function will take a scale and find a mode (or modes), based upon some consonance metric function. Here is one such object, which is implemented as a Python dict.

```
{'mask': (0, 2, 3, 5, 7, 9, 10, 12),
'metric_3': 22.1402597402597,
'original_scale': [1,
 256/243,
 9/8,
 32/27,
 81/64,
 4/3,
 1024/729,
 3/2,
 128/81,
 27/16,
 16/9,
 243/128,
 21,
'scale': [1, 9/8, 32/27, 4/3, 3/2, 27/16, 16/9, 2],
'steps': [2, 1, 2, 2, 2, 1, 2],
'sum_distinct_intervals': 12,
'sum_p_q': 161,
'sum_p_q_for_all_intervals': 4374,
'sum_q_for_all_intervals': 1822}
```

The meaning of these keys:

- original\_scale is the original scale which was input into the function. In this example is was a Pythagorean scale.
- scale is the output scale of the function
- mask is the mask of the original scale that produces the output
- steps is similar to mask, but reported in a different format. Each entry in the steps list represents the number of degrees in the original scale between successive degrees in the returned scale. The standard major scale, for example, would be represented by [2, 2, 1, 2, 2, 2, 1].

In this example there are also other keys included.  $sum_distinct_intervals$ ,  $sum_p_q$ ,  $sum_p_q$ for\_all\_intervals,  $sum_q$ for\_all\_intervals, and metric\_3 are the outputs of calculated metric functions. This particular mode, for example, has a rating of 161 by the  $sum_p_q$  metric.

Metric functions are describe briefly below, and in more detail in *Metric Functions*.

# 3.1.5 Tuning Tables

*Tuning Tables* are a representation of a scale, usually a string (which can be written to a file), which can be understood by an external software package. As an example, to take a standard Pythagorean scale and produce a representation understood by Scala:

```
pythag_scale = create_pythagorean_scale()
scala_tuning_table = create_scala_tuning(pythag_scale, "Pythagorean Scale")
```

The variable scala\_tuning\_table now contains the following:

```
! Scale produced by pytuning. For tuning yoshimi or zynaddsubfx,
! only include the portion below the final '!'
Pythagorean Scale
12
256/243
9/8
32/27
81/64
4/3
1024/729
3/2
128/81
27/16
16/9
243/128
2/1
```

For many tuning tables one has to pin the scale to some reference frequency. For this the convention of MIDI note number is employed. For example, in the MIDI standard the note 69 is A 440 Hz, so by specifying a reference of 69, the corresponding entry in the table would be 400 Hz, and this would represent the root or tonic degree of the scale.

Exporting the above scale in a Csound compatible format:

```
csound_tuning_table = create_csound_tuning(pythag_scale, reference_note=69)
```

### yields the following:

f1 0 256 -2	8.14815 8.70117	9.16667	9.65706	10.31250	10.86420
→ 11.60156	12.22222 \				
	13.05176 13.75000	14.48560	15.46875	16.29630	17.40234
→ 18.33333	19.31413 \				
	20.62500 21.72840	23.20313	24.4444	26.10352	27.50000
→ 28.97119	30.93750 \				
	32.59259 34.80469	36.66667	38.62826	41.25000	43.45679
→ 46.40625	48.88889 \				
	52.20703 55.00000	57.94239	61.87500	65.18519	69.60938 _
→ 73.33333	77.25652 \				
	82.50000 86.91358	92.81250	97.77778	104.41406	110.00000
<b>→</b> 115.88477	123.75000 \				
	130.37037 139.21875	146.66667	154.51303	165.00000	173.82716
<b>→</b> 185.62500	195.55556 \				
	208.82813 220.00000	231.76955	247.50000	260.74074	278.43750
<b>→</b> 293.33333	309.02606 \				
	330.00000 347.65432	371.25000	391.11111	417.65625	440.00000
<b>463.53909</b>	495.00000 \				
	521.48148 556.87500	586.66667	618.05213	660.00000	695.30864 _
→742.50000	782.22222 \				
	835.31250 880.00000	927.07819	990.00000	1042.96296	1113.75000 _
<b>→</b> 1173.33333	1236.10425 \				
	1320.00000 1390.61728	1485.00000	1564.44444	1670.62500	1760.00000 _
<b>→</b> 1854.15638	1980.00000 \				
	2085.92593 2227.50000	2346.66667	2472.20850	2640.00000	2781.23457 _
<b>→</b> 2970.00000	3128.88889 \				
	3341.25000 3520.00000	3708.31276	3960.00000	4171.85185	4455.00000 _
<b>→</b> 4693.33333	4944.41701 \				
	5280.00000 5562.46914	5940.00000	6257.77778	6682.50000	7040.00000 _
→7416.62551	7920.00000 \				

```
8343.70370 8910.00000 9386.66667 9888.83402 10560.00000 11124.93827

→11880.00000 12515.55556
```

This is a 128-entry table, mapping note number to absolute frequency. Csound's table opcode can be used to index into the table and play the appropriate frequency, using something like the following:

```
inote init p4
iveloc init p5
ifreq table inote, 1
al oscil iveloc, ifreq, 2
outs al, al
```

(This assumes that p4 in the orchestra file contains MIDI note numbers, of course. If you use a different convention there are translation opcodes that can be used.)

#### 3.1.6 Metric Functions

Metric Functions are functions that takes a scale as an input and returns a numeric value calculated from that scale. It is used, for example, in find\_best\_modes() to evaluate the consonance of a scale (find\_best\_modes() uses a metric to evaluate the consonance of all possible modes of a scale and returns the evaluation of those modes as a mode object).

The return value of a metric function should be a dict with a unique string identifier as the key and the metric as the value.

As an example, the following is one of the package-defined metrics:

```
pytuning.metrics.sum_p_q_for_all_intervals(scale)
Calculate a metric for a scale
```

Parameters scale - The scale (i.e., a list of sympy. Rational values)

Returns The metric.

This metric is an estimate of scale consonance. It is formed by examining all unique intervals in the scale, and creating a numeric value based upon the summation of the numerators and denominators for all those intervals.

While the metric is numerically defined for ratios expressed as irrational or transcendental numbers, it is really only meaningful for scales with just degrees (ratios expressed as rational numbers).

Smaller values are more consonant.

As an example of use, the following:

```
pythag = create_pythagorean_scale()
metric = sum_p_q_for_all_intervals(pythag)
```

yields the following:

```
{'sum_p_q_for_all_intervals': 1092732}
```

## 3.2 Scale Creation

There are several scale-creation functions in the package. They are found in pytuning.scales and can be imported into the program's namespace with

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```
from pytuning.scales import *
```

(Note that for interactive use these are imported by default).

#### 3.2.1 The Harmonic Scale

We'll start with the harmonic scale; it will illustrate many of the concepts used in scale creation.

There are two important concepts to understand:

- Normalization: If a scale is normalized (which is the default in all cases), then the intervals of the scale are normalized to fall within a single octave. This means scaling the interval either up or down the number of octaves needed to make the interval fall between the unison and the octave.
- The Octave: Normally an octave is defined as a doubling of frequency (2), but it is possible to define an octave by some other number. If this is the case the normalization will takes place over this new octave.

The function to create a harmonic scale is, create harmonic scale:

pytuning.scales.create\_harmonic\_scale (first\_harmonic, last\_harmonic, normalize=True, octave=2)

Create a harmonic scale

#### **Parameters**

- first harmonic The first harmonic
- last harmonic The last harmonic
- normalize If true, normalize the scale to an octave (2/1 by default, otherwise taken from octave)
- octave The definition of the formal octave.

**Returns** The scale

As an example of use, a normalized scale constructed from harmonics 3 to 20:

```
scale = create_harmonic_scale(3,20)
```

which yields:

$$\left[1, \frac{13}{12}, \frac{7}{6}, \frac{5}{4}, \frac{4}{3}, \frac{17}{12}, \frac{3}{2}, \frac{19}{12}, \frac{5}{3}, \frac{11}{6}, 2\right]$$

To create a non-normalized scale:

```
scale = create_harmonic_scale(3,10, normalize=False)
```

which yields:

$$\left[1, \frac{4}{3}, \frac{5}{3}, 2, \frac{7}{3}, \frac{8}{3}, 3, \frac{10}{3}\right]$$

As an example, if we create a non-normalized harmonic scale of 10 harmonics:

```
harmonic_scale = create_harmonic_scale(1, 10, normalize=False)
```

We have the following scale:

If we normalize it each interval is scaled by a power of two to fall within 1 and 2. So, for example, the 9 becomes  $\frac{9}{8}$ , because the nine must be scaled by three octaves to fall within that range:

$$\frac{9}{8} = \frac{9}{2^3}$$

So the normalized scale is:

$$\left[1, \frac{9}{8}, \frac{5}{4}, \frac{3}{2}, \frac{7}{4}, 2\right]$$

But if we change our octave definition to be 3, we normalize on powers of 3:

```
harmonic_scale = create_harmonic_scale(1, 10, octave=3)
```

yields:

$$\[1, \quad \frac{10}{9}, \quad \frac{4}{3}, \quad \frac{5}{3}, \quad 2, \quad \frac{7}{3}, \quad \frac{8}{3}, \quad 3\]$$

# 3.2.2 Equal Divsion of the Octave (Equal Temprament)

Equal temperament scales can be created with the <code>create\_edo\_scale()</code> function. Note that this function does not accept a <code>normalize</code> argument, because EDO scales are normalized by definition. If does, however, allow you to change the definition of the formal octave.

pytuning.scales.create edo scale(number tones, octave=2)

Create an equal division of octave (EDO, ET) scale.

#### **Parameters**

- number\_tones The number of tones/divisions in the scale
- octave The formal octave (frequency ratio)

Example, 12T-ET:

```
edo_scale = create_edo_scale(12)
```

will yield the normal equal-tempered scale used in western music:

$$\left[1,\ \sqrt[12]{2},\sqrt[6]{2},\sqrt[4]{2},\sqrt[3]{2},2^{\frac{5}{12}},\sqrt{2},2^{\frac{7}{12}},2^{\frac{2}{3}},2^{\frac{3}{4}},2^{\frac{5}{6}},2^{\frac{11}{12}},2\right]$$

Note that the length of the scale is 13, as both the unison and octave are included by convention.

It is also possible to have a non-2 formal octave. The code:

```
edo_scale = create_edo_scale(12,3)
```

will yield:

$$\left[1, \sqrt[12]{3}, \sqrt[6]{3}, \sqrt[4]{3}, \sqrt[3]{3}, 3^{\frac{5}{12}}, \sqrt{3}, 3^{\frac{7}{12}}, 3^{\frac{2}{3}}, 3^{\frac{3}{4}}, 3^{\frac{5}{6}}, 3^{\frac{11}{12}}, 3\right]$$

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### 3.2.3 Scales from a Generator Interval

The create\_equal\_interval\_scale() function will generate a scale from a generator interval. This is the base function for several other scale types (for example, the Pythagorean scale is created with a generator interval of  $\frac{3}{2}$ ).

In he creation of a scale, the generator interval can either be used directly (for, for example, making each successive tone a generator interval above the previous tone), or in an inverted sense (making each interval a generator *down* from the previous). This function starts from the unison and walks down the number specified, walking up for the rest of the intervals.

```
pytuning.scales.create_equal_interval_scale(generator_interval, scale_size=12, number_down_intervals=6, epsilon=None, sort=True, octave=2, remove duplicates=True, normalize=True)
```

Create a scale with equal-interval tuning

#### **Parameters**

- **generator\_interval** The interval to use for generation (sympy value)
- scale\_size The number of degrees in the scale
- number\_down\_intervals The number of inverted intervals to use in scale construction.
- **epsilon** Rounding parameter. If set to None no rounding is done. Otherwise the scale degrees are rounded to the nearest epsilon
- sort If True, sort the output by degree size
- octave The formal octave
- remove\_duplicates If True remove duplicate entries
- normalize IF True, normalize the degrees to the octave

In general one should keep epsilon at None and perform and rounding outside the function.

This is a base function from which several other scales are derived, including:

•The Pythagorean scale A scale with a perfect fifth (3/2) as the generating interval

$$P_5 = \frac{3}{2}$$

•The quarter-comma meantone scale A scale in which the generating interval is a perfect fifth narrowed by one quarter of syntonic comma

$$P_5 = \frac{\frac{3}{2}}{\sqrt[4]{\frac{81}{80}}}$$

•**EDO Scales** EDO scales can be generated from an appropriate selection of the fifth. For example, the 12-TET scale would use the fifth:

$$P_5 = \frac{7}{18}\sqrt{2}$$

# 3.2.4 The Pythagorean Scale

This is the standard Pythagorean scale. Note that we can choose the number of up and down intervals in the scale. The default yields the standard scale, with the fourth degree as a diminished fifth, as opposed to the augmented fourth.

```
pytuning.scales.create_pythagorean_scale(scale_size=12, number_down_fifths=6, ep-
silon=None, sort=True, octave=2, re-
move_duplicates=True)
```

Create a Pythagorean scale

#### **Parameters**

- scale\_size The number of degrees in the scale
- number\_down\_fifths The number of inverted fifths to use in scale construction.
- **epsilon** Rounding parameter. If set to None no rounding is done. Otherwise the scale degrees are rounded to the nearest epsilon
- sort If True, sort the output by degree size
- octave The formal octave
- remove\_duplicates If True remove duplicate entries

The Pythagorean scale is an even-interval scale with the following generating interval:

$$P_5 = \frac{3}{2}$$

So, for the standard scale we can use:

```
scale = create_pythagorean_scale()
```

yielding:

$$\left[1, \quad \frac{256}{243}, \quad \frac{9}{8}, \quad \frac{32}{27}, \quad \frac{81}{64}, \quad \frac{4}{3}, \quad \frac{1024}{729}, \quad \frac{3}{2}, \quad \frac{128}{81}, \quad \frac{27}{16}, \quad \frac{16}{9}, \quad \frac{243}{128}, \quad 2\right]$$

If we wanted the augmented fourth:

```
scale = create_pythagorean_scale(number_down_fifths=5)
```

yielding:

$$\left[1, \quad \frac{256}{243}, \quad \frac{9}{8}, \quad \frac{32}{27}, \quad \frac{81}{64}, \quad \frac{4}{3}, \quad \frac{729}{512}, \quad \frac{3}{2}, \quad \frac{128}{81}, \quad \frac{27}{16}, \quad \frac{16}{9}, \quad \frac{243}{128}, \quad 2\right]$$

### 3.2.5 The Quarter-Comma Meantone Scale

```
pytuning.scales.create_quarter_comma_meantone_scale (scale\_size=12, num-ber\_down\_fifths=6, ep-silon=None, sort=True, octave=2, re-move\_duplicates=True)
```

Create a quarter-comma meantone scale

#### **Parameters**

• scale\_size - The number of degrees in the scale

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- number down fifths The number of inverted fifths to use in scale construction.
- **epsilon** Rounding parameter. If set to None no rounding is done. Otherwise the scale degrees are rounded to the nearest epsilon
- sort If True, sort the output by degree size
- octave The formal octave
- remove\_duplicates If True remove duplicate entries

The quarter-comma meantone scale is an even-interval scale with the following generating interval:

$$P_5 = \frac{\frac{3}{2}}{\sqrt[4]{\frac{81}{80}}}$$

which is a perfect fifth (in a Pythagorean sense) narrowed by one quarter of the syntonic comma.

An example of use:

```
scale = create_quarter_comma_meantone_scale()
```

yields:

$$\left[1, \quad \frac{8}{25}5^{\frac{3}{4}}, \quad \frac{\sqrt{5}}{2}, \quad \frac{4\sqrt[4]{5}}{5}, \quad \frac{5}{4}, \quad \frac{2}{5}5^{\frac{3}{4}}, \quad \frac{16\sqrt{5}}{25}, \quad \sqrt[4]{5}, \quad \frac{8}{5}, \quad \frac{5^{\frac{3}{4}}}{2}, \quad \frac{4\sqrt{5}}{5}, \quad \frac{5\sqrt[4]{5}}{4}, \quad 2\right]$$

## 3.2.6 Euler-Fokker Genera

pytuning.scales.create\_euler\_fokker\_scale(intervals, multiplicities, octave=2, normal-ize=True)

Create a scale in the Euler-Fokker Genera

#### **Parameters**

- intervals The factors to use for the construction (usually prime numbers)
- multiplicities The multiplicities of the factors (see below)
- octave The formal octave
- normalize If True, normalize the intervals to the octave.

intervals and multiplicities should both be lists of equal length. The entries in multiplicities give the number of each factor to use. Therefore the following:

```
intervals = [3,5,7]
multiplicities = [1,1,1]
scale = create_euler_fokker_scale(intervals, multiplicities)
```

Will create a scale with one 3, one 5, and one 7 as generators.

The above will produce the following scale:

$$\left[1, \frac{35}{32}, \frac{5}{4}, \frac{21}{16}, \frac{3}{2}, \frac{105}{64}, \frac{7}{4}, \frac{15}{8}, 2\right]$$

Also note that the two statements will generate the same output:

```
intervals = [3,5,7]
multiplicities = [2,2,1]
scale1 = create_euler_fokker_scale(intervals, multiplicities)

intervals = [3,3,5,5,7]
multiplicities = [1,1,1,1,1]
scale2 = create_euler_fokker_scale(intervals, multiplicities)

scale1 == scale2
True
True
```

#### 3.2.7 Diatonic Scales

 $\verb|pytuning.scales.create_diatonic_scale| (\textit{generators}, \textit{specification})|$ 

Create a diatonic scale.

#### **Parameters**

- **generators** The generator intervals (see below)
- **specification** The scale specification. This is a list of chars that correspond to entries in the generators. Note that if all the character representations are a single character, you can pass the specification in as a string for convenience.

**Returns** The specified scale

generators is a list of tuples, the first member of which is an interval specification, the second of which is a character representation. The entries in specification should correspond to this value.

As an example, we can create the 12 EDO generators thus:

```
edo12_constructors = [
    (sp.power.Pow(2,sp.Rational(2,12)), "T"),
    (sp.power.Pow(2,sp.Rational(1,12)), "s"),
]
```

We can then create the standard major mode with:

```
create_diatonic_scale(edo12_constructors, ["T","T","s","T","T","T","s"])
```

which will yield:

$$\left[1, \quad \sqrt[6]{2}, \quad \sqrt[3]{2}, \quad 2^{\frac{5}{12}}, \quad 2^{\frac{7}{12}}, \quad 2^{\frac{3}{4}}, \quad 2^{\frac{11}{12}}, \quad 2\right]$$

As another example of creating a diatonic scale, we can use the five-limit constructors (which are defined in pytuning.constants):

```
five_limit_constructors = [
          (sp.Rational(16,15), "s"),
          (sp.Rational(10,9), "t"),
          (sp.Rational(9,8), "T"),
]
```

to create Ptolemy's Intense Diatonic Scale:

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```
from pytuning.constants import five_limit_constructors
from pytuning.scales import create_diatonic_scale

scale = create_diatonic_scale(five_limit_constructors,
    ["T", "t", "s", "T", "t", "s"])
```

which gives us:

$$\left[1, \quad \frac{9}{8}, \quad \frac{5}{4}, \quad \frac{4}{3}, \quad \frac{3}{2}, \quad \frac{5}{3}, \quad \frac{15}{8}, \quad 2\right]$$

Note that if every identifier is a single-character string, specification can also be passed in as a string. So this is equivalent:

```
from pytuning.constants import five_limit_constructors
from pytuning.scales import create_diatonic_scale

scale = create_diatonic_scale(five_limit_constructors, "TtsTtTs")
```

# 3.3 Metric Functions

A **metric function** is a function that takes a scale as input and returns a calculated value. As mentioned in *Basic Concepts*, it returns a Python dict with the metric name as the key, and the metric value as the value.

The currently defined metrics all estimate the consonance or dissonance of a scale.

# 3.3.1 sum\_p\_q()

pytuning.metrics.sum\_p\_q(scale)

Calculate a metric for a scale

**Parameters** scale – The scale.

**Returns** A dict with the metric value.

This is an estimate of scale consonance. It is derived from summing the numerators and denominators of the scale degrees.

Smaller values are more consonant.

Note that this metric looks at the degrees of the scale, so it is somewhat tonic-focused. The similar metric sum\_p\_q\_for\_all\_intervals() is similar, but it sums the numerator and denominator values for all distinct intervals within the scale.

While the metric is numerically defined for ratios expressed as irrational or transcendental numbers, it is really only meaningful for scales with just degrees (ratios expressed as rational numbers).

```
sum_p_q(create_pythagorean_scale())
```

yields:

```
{'sum_p_q': 3138}
```

## 3.3.2 sum distinct intervals()

pytuning.metrics.sum\_distinct\_intervals(scale)

Calculate a metric for a scale

Parameters scale - The scale.

**Returns** A dict with the metric value.

This metric is an estimate of scale consonance. Numerically it is the number of distinct intervals within the scale (including all ratios and their inversions).

Smaller values are more consonant.

```
sum_distinct_intervals(create_pythagorean_scale())
```

yields:

```
{'sum_distinct_intervals': 22}
```

# 3.3.3 metric\_3()

pytuning.metrics.metric\_3 (scale)

Calculate a metric for a scale

Parameters scale - The scale.

**Returns** A dict with the metric value.

Metric 3 is an estimate of scale consonance. Given a ratio p/q, it is a heuristic given by the following:

$$m_3 = \sum \frac{1}{\frac{p-q}{q}}$$
 
$$= \sum \frac{q}{p-q}$$
 (3.1)

Smaller values are more consonant.

The summation takes place over all of the intervals in the scale. It does not form a set of distinct intervals.

# 3.3.4 sum\_p\_q\_for\_all\_intervals()

```
pytuning.metrics.sum_p_q_for_all_intervals(scale)
```

Calculate a metric for a scale

Parameters scale - The scale (i.e., a list of sympy. Rational values)

Returns The metric.

This metric is an estimate of scale consonance. It is formed by examining all unique intervals in the scale, and creating a numeric value based upon the summation of the numerators and denominators for all those intervals.

While the metric is numerically defined for ratios expressed as irrational or transcendental numbers, it is really only meaningful for scales with just degrees (ratios expressed as rational numbers).

Smaller values are more consonant.

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# 3.3.5 sum\_q\_for\_all\_intervals()

```
pytuning.metrics.sum_q_for_all_intervals(scale)
Calculate a metric for a scale.
```

Parameters scale - The scale (i.e., a list of Rational s)

Returns The metric.

Metric 5 is an estimate of scale consonance. It is summation of the denominators of the normalized distinct ratios of the scale.

Smaller values are more consonant.

# 3.3.6 All Metrics

There is also a function that calculates all defined metrics for a scale.

```
pytuning.metrics.all_metrics(scale)
```

Calculate all metrics for the scale

**Parameters** scale – The scale (i.e., a list of Rational s)

**Returns** A dict containing all metrics.

As an example:

```
pythag = create_pythagorean_scale()
metrics = all_metrics(pythag)
```

will (currently) produce:

```
{
  'metric_3': 49.9049074891784,
  'sum_distinct_intervals': 22,
  'sum_p_q': 3138,
  'sum_p_q_for_all_intervals': 1092732,
  'sum_q_for_all_intervals': 452817
}
```

If new metrics are coded they should be added to the \_\_\_all\_\_ data member for inclusion here.

# 3.4 Scale Analysis and Creation (Redux)

*Scale Creation* describes the way that many standard scales are generated from within the package. But there are other ways to create scales.

#### 3.4.1 Mode Selection

When one creates a scale – for example, the Pythagorean scale or a scale of the Euler-Fokker Genera – one can looks at the various modes that can be created for that scale and evaluate them by certain criteria.

The find\_best\_modes () function can be used for this. This function accepts and input scale, the number of tones for the mode, and the optimization functions that should be used for evaluating the scale.

As an example, one scale that's I've used in compositions is created from choosing a seven-note mode from a harmonic scale, optimized over the metric sum\_p\_q\_for\_all\_intervals(). This particular scale is based upon the harmonic series referenced to the fourth harmonic.

The following code:

yields the following object:

```
[{'mask': (0, 2, 4, 5, 8, 12, 14, 15),
  'original_scale': [1,
  17/16,
  9/8,
  19/16,
  5/4,
  21/16,
  11/8,
  23/16,
  3/2,
  25/16,
  13/8,
  27/16,
  7/4,
  29/16,
  15/8,
 'scale': [1, 9/8, 5/4, 21/16, 3/2, 7/4, 15/8, 2],
 'steps': [2, 2, 1, 3, 4, 2, 1],
 'sum_p_q_for_all_intervals': 572}]
```

The returned scale:

$$\left[1, \quad \frac{9}{8}, \quad \frac{5}{4}, \quad \frac{21}{16}, \quad \frac{3}{2}, \quad \frac{7}{4}, \quad \frac{15}{8}, \quad 2\right]$$

minimizes the metric for all possible combinations of 7 notes chosen from the original harmonic scale.

Find the best modes for a scale, as defined by the specified metrics.

#### **Parameters**

- scale The scale to analyze
- num\_tones The number of degrees in the mode
- sort\_order How the return should be sorted, referenced to the metrics calculated
- num\_scales The number of scales to return. If None all scales will be returned
- metric\_function The metric function to use. If None then all\_metrics will be used.

**Returns** A sorted list of mode objects.

The sort order is a list of keys that the metric function should return, applied in order, with an assumption that the lower the metric the more consonant (and "better") the scale. As an example, the default sort order:

```
['sum_p_q_for_all_intervals','sum_p_q','sum_distinct_intervals']
```

Will order the scales by increasing **sum\_p\_q\_for\_all\_intervals**. If two scales have the same **sum\_p\_q** value they will be secondarily sorted on **sum\_p\_q**. If scales have the same **sum\_p\_q\_for\_all\_intervals** and **sum\_p\_q** then **sum\_distinct\_intervals** will be used.

If no metric function is specified the default all\_metrics will be used. However, for efficiency one may not want to calculate all metrics if they are not being used. For example, if one is just interested in one metric, you can pass the metric directly:

which would yield:

```
[{'mask': (0, 1, 3, 5, 6, 8, 10, 12),
  'original_scale': [1,
  256/243,
  9/8,
  32/27,
  81/64,
  4/3,
  1024/729,
  3/2,
  128/81,
  27/16,
  16/9,
  243/128,
  'scale': [1, 256/243, 32/27, 4/3, 1024/729, 128/81, 16/9, 2],
 'steps': [1, 2, 2, 1, 2, 2, 2],
  'sum_p_q_for_all_intervals': 4374}]
```

If one is interested in two of the metrics, you could, for example:

which would yield:

```
[{'mask': (0, 2, 3, 5, 7, 9, 10, 12),
  'original_scale': [1,
  256/243,
  9/8,
  32/27,
  81/64,
  4/3,
  1024/729,
  3/2,
  128/81,
  27/16,
  16/9,
  243/128,
  2],
  'scale': [1, 9/8, 32/27, 4/3, 3/2, 27/16, 16/9, 2],
  'steps': [2, 1, 2, 2, 2, 1, 2],
 'sum_p_q': 161,
  'sum_p_q_for_all_intervals': 4374}]
```

# 3.4.2 Factoring an Interval

Sometimes it is interesting to take an interval and find an expression for that interval over some set of generator intervals. For this the function find\_factors() is provided.

One has to specify the generator intervals. This is done by passing the function a list of tuples. Each tuple has two members: The generator interval, and a character representation of the generator interval. Usually these are a single, unique character (such as X), but it can also be in the form 1/X. If it is in this form the generator interval should be the reciprocal of the interval designated by X.

As an example, we could create a generator interval that represents the tone and semi-tone of a 31-EDO scale:

```
edo31_constructors = [
    (sp.power.Pow(2,sp.Rational(2,31)), "T"), # a tone
    (sp.power.Pow(2,sp.Rational(1,31)), "s"), # a semitone
]
```

(Note that the tone is just twice the semitone, so we could probably get by with just defining the semitone).

Now we can define an interval, say, one of the intervals of the Pythagorean scale:

 $\frac{21}{16}$ 

and see what factoring yields an interval closest to the original.

```
results = find_factors(interval, edo31_constructors)
results
```

results now contains the factoring, the factoring in symbolic terms, and the resultant interval.

```
([2**(2/31), 2**(2/31), 2**(2/31), 2**(2/31), 2**(2/31), 2**(2/31)],

['T', 'T', 'T', 'T', 'T'],

2**(12/31))
```

The last entry is the returned interval:

 $2^{\frac{12}{31}}$ 

If one is interested in seeing how closely the factored interval matches the original interval, the ratio\_to\_cents() function in pytuning.utiities can be used.

```
from pytuning.utilities import ratio_to_cents
print(ratio_to_cents(results[2] / interval))
```

yields:

```
-6.26477830225428
```

In other words, the derived interval is flat about 6.3 cents from the target interval.

```
pytuning.utilities.ratio_to_cents(ratio)
```

Convert a scale degree to a cent value

Parameters ratio - The scale degree (sympy value)

**Returns** The scale degree in cents

Calculates:

$$\sqrt[2]{\frac{1}{1200}}\sqrt{\text{degree}}$$

Note that this function returns a floating point number, not a sympy ratio.

# 3.4.3 Approximating a Scale with Another Scale

The above factoring of an interval over a set of generators can be extended: a scale can be factored too.

To do this the <code>create\_scale\_from\_scale()</code> function is used.

The first step in using this function is to create an interval function. It is similar to find\_factors() in that it accepts an interval and a max factor, and it returns the factor. But the actual generator intervals are bound to this function.

The easiest way of creating this function is to take the generator intervals that you're interested in and to bind them to find\_factors() via a partial function application. As an example, we can take the five-limit constructors:

```
five_limit_constructors = [
    (sp.Rational(16,15), "s"),
    (sp.Rational(10,9), "t"),
    (sp.Rational(9,8), "T"),
]
```

And use them to approximate the Pythagorean scale:

```
from pytuning.scales import create_pythagorean_scale
from pytuning.scale_creation import create_scale_from_scale, find_factors
from pytuning.constants import five_limit_constructors
from functools import partial

interval_function = partial(find_factors, constructors=five_limit_constructors)
pythag = create_pythagorean_scale()
results = create_scale_from_scale(pythag, interval_function)
```

The return value is a tuple, the first element of which is derived scale, the second of which is the symbolic factoring. The scale which was found was

$$\left[1, \quad \frac{16}{15}, \quad \frac{9}{8}, \quad \frac{32}{27}, \quad \frac{81}{64}, \quad \frac{4}{3}, \quad \frac{1024}{729}, \quad \frac{3}{2}, \quad \frac{128}{81}, \quad \frac{27}{16}, \quad \frac{16}{9}, \quad \frac{243}{128}, \quad 2\right]$$

If you look at the Pythagorean scale:

$$\left[1, \quad \frac{256}{243}, \quad \frac{9}{8}, \quad \frac{32}{27}, \quad \frac{81}{64}, \quad \frac{4}{3}, \quad \frac{1024}{729}, \quad \frac{3}{2}, \quad \frac{128}{81}, \quad \frac{27}{16}, \quad \frac{16}{9}, \quad \frac{243}{128}, \quad 2\right]$$

you can see that they only differ in the second degree (which if we look at the first member of the return we can see is factored as ['s']). Looking at how much they differ:

```
ratio = results[0][1] / pythag[1]
print(ratio)
81/80
print(ratio_to_name(ratio))
Syntonic Comma
delta = ratio_to_cents(ratio)
print(delta)
21.5062895967149
```

we see that the difference is  $\frac{81}{80}$ , which is the syntonic comma (about 21.5 cents).

create\_scale\_from\_scale() can also accept a tone\_table which is a list of the potential breakdowns that can be used in the analysis.

```
pytuning.scale_creation.create_scale_from_scale(scale, interval_function, max_terms=8, tone table=None)
```

Given a target scale, calculate the closest matching N-rank linear temperament scale over the provide basis functions.

#### **Parameters**

- scale The target scale (list or ratios)
- interval\_function The interval function (see below)
- max\_terms The maximum number of terms for the factoring along the basis intervals
- tone table A constrained tone table (see below)

**Returns** A tuple, the first member of which is a list of the derived scale values, and the second of which is a symbolic representation of the factoring found.

The interval function is a function that accepts a degree and max\_terms and returns the breakdown in the same format as find\_factors. In general the easiest way to create this function is thought a partial function application of find\_factors and the specific constructors wanted. As an example, to create a function that will approimate a scale with the five-limit constructors:

if tone\_table is None, the code will perform the factoring with up to max\_terms. If the tone table is defined only the intervals defined in this table will be used.

The tone table is formatted as a list of tuples, where the members of each tuple are the degree name (String), the interval composition (a list of characters taken from the symbolic portion of the constructors), and the value of that factoring. As an example, the tone table that matches published values for the Lucy-tuned scale begins:

```
[('1', [], 1),

('5', ['L', 'L', 'L', 's'], sqrt(2)*2**(1/(4*pi))),

('2', ['L'], 2**(1/(2*pi))),

('6', ['L', 'L', 'L', 's'], sqrt(2)*2**(3/(4*pi))),

('3', ['L', 'L'], 2**(1/pi)),

('7', ['L', 'L', 'L', 'L', 's'], sqrt(2)*2**(5/(4*pi))),

('#4', ['L', 'L', 'L'], 2**(3/(2*pi))), ...]
```

(The last member of the tuple is a sympy symbolic value.)

With the tone table, the code will return the defined tone which most closely matches the target degree.

Extending the above example, if we were to try to match a Pythagorean scale with an unconstrained factoring of the Five-limit intervals (i.e., with no tone table):

```
pythag = create_pythagorean_scale()
lp = create_five_limit_scale_from_scale(pythag)
```

#### yields

```
([1,
 16/15,
 9/8,
 32/27,
 81/64,
 4/3,
 1024/729,
 3/2,
 128/81,
 27/16,
 16/9,
 243/128,
 2],
 [[],
 ['s'],
  ['T'],
  ['s', 't'],
  ['T', 'T'],
  ['T', 's', 't'],
  ['s', 's', 't', 't'],
  ['T', 'T', 's', 't'],
  ['T', 's', 's', 't', 't'],
  ['T', 'T', 'T', 's', 't'],
  ['T', 'T', 's', 's', 't', 't'],
       'T', 'T', 'T', 's', 't'],
  ['T', 'T', 'T', 's', 's', 't', 't']])
```

Note that the first entry of the factors is always for the ratio 1, and is returned as an empty list (as there really *are* no factors in this sense).

# 3.5 Tuning Tables

A **tuning table** is a text representation of a scale that can be interpreted by an external program. This is usually used to tune a synthesizer or other sound source so that the scale can be used in a musical composition.

Some tuning tables – such as that used by Scala – describe the scale in absolute terms, but most need to have a reference defined so that the scale degrees can be mapped to a frequency. For this purpose the PyTuning package has adopted

Octave	С	C#	D	D#	E	F	F#	G	G#	Α	A#	В
-2	0	1	2	3	4	5	6	7	8	9	10	11
-1	12	13	14	15	16	17	18	19	20	21	22	23
0	24	25	26	27	28	29	30	31	32	33	34	35
1	36	37	38	39	40	41	42	43	44	45	46	47
2	48	49	50	51	52	53	54	55	56	57	58	59
3	60	61	62	63	64	65	66	67	68	69	70	71
4	72	73	74	75	76	77	78	79	80	81	82	83
5	84	85	86	87	88	89	90	91	92	93	94	95
6	96	97	98	99	100	101	102	103	104	105	106	107
7	108	109	110	111	112	113	114	115	116	117	118	119
8	120	121	122	123	124	125	126	127				

the MIDI standard for note numbers and frequencies.

So, for example, note number 69 corresponds to middle A, whereas 60 corresponds to middle C. The frequency standard is 12-EDO, and the note 69 is pegged to 440 Hz. Thus if you passed 69 as the reference note, the 69'th entry in the table would be 440 Hz and this would correspond to the first degree of the scale. 60 would cause the first degree of the scale to be assigned to that note number (with a corresponding frequency of about 261.6 Hz). The timidity soft synth is an example of a synthesizer that needs this reference note and frequency.

In general the table will need to be output to disk so that it can read by the program. This can be done with something like:

```
from pytuning.tuning_tables import create_timidity_tuning
from pytuning.scales import create_euler_fokker_scale

reference_note = 60
scale = create_euler_fokker_scale([3,5],[3,1])

tuning = create_timidity_tuning(scale, reference_note=reference_note)

with open("timidity.table", "w") as table:
    table.write(tuning)
```

This will cause the generated scale:

$$\left[1, \quad \frac{135}{128}, \quad \frac{9}{8}, \quad \frac{5}{4}, \quad \frac{45}{32}, \quad \frac{3}{2}, \quad \frac{27}{16}, \quad \frac{15}{8}, \quad 2\right]$$

to be written to a disk file, timidity.table, which can be understood by timidity:

```
timidity -Z timidity.table score.mid
```

# 3.5.1 Timidity

```
pytuning.tuning_tables.create_timidity_tuning(scale, reference_note=60)

Create a Timidity++ tuning table
```

#### **Parameters**

- **scale** The scale to model (list of frequency ratios)
- reference\_note The MIDI number of the absolute frequency reference

Returns A Timidity tuning table as a String

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The default value of reference\_note pegs the scale to to the standard concert tuning of middle C (A = 440Hz).

The Timidity table is basically a list of integers for all defined MIDI note numbers, with each entry as 1000 times the note frequency

As a somewhat detailed example, let's say that the user had a 12-EDO scale constructed, and wanted to pin the tonic note to the standard A440. The following will do this:

```
from pytuning.scales import create_edo_scale
from pytuning.tuning_tables import create_timidity_tuning

scale = create_edo_scale(12)
tuning_table = create_timidity_tuning(scale, reference_note=69)
```

with the first part of the table given by:

```
# Timidity tuning table created by pytuning,
# call timidity with the -Z option to enable.
# Note reference: 69; Freq reference: 440.000000 Hz
8176
8662
9177
9723
10301
10913
11562
12250
12978
```

To use the table, one starts Timidity with the **-Z** option, i.e:

```
timidity -Z table.name -iA
```

## 3.5.2 Scala

The Scala tuning table can be used with the Scala package, but it can also be used to tune the soft synth Zynaddsubfx, as well as its derivative Youshimi. With the soft synths you will need to explicitly set the reference note and frequency in the scale GUI.

```
pytuning.tuning_tables.create_scala_tuning(scale, name)
Create a Scala scale file
```

#### **Parameters**

- scale The scale (list of frequency ratios)
- name The name of the scale

Returns A Scala file as a String

The Scala file can be used to tune various things, most germane being Yoshimi. However, keep in mind that the Scala file does **not** include a base note or frequency, so for tuning purposes those data will need to be captured or input in some other way.

As an example of use, the Scala file for the default Pythagorean tuning can be calculated thus:

```
from pytuning.scales.pythagorean import create_pythagorean_scale
from pytuning.tuning_tables import create_scala_tuning
```

```
scale = create_pythagorean_scale()
table = create_scala_tuning(scale,"Pythagorean Tuning")
```

#### which yields:

```
! Scale produced by pytuning. For tuning yoshimi or zynaddsubfx,
! only include the portion below the final '!'
Pythagorean Tuning
12
256/243
9/8
32/27
81/64
4/3
1024/729
3/2
128/81
27/16
16/9
243/128
2/1
```

Note that the Scala file uses exact ratios where possible, otherwise it will convert to a cent value. Thus the code:

```
from pytuning.scales import create_edo_scale
from pytuning.tuning_tables import create_scala_tuning

scale = create_edo_scale(12)
table = create_scala_tuning(scale, "12-TET Tuning")
```

### will produce:

```
! Scale produced by pytuning. For tuning yoshimi or zynaddsubfx,
! only include the portion below the final '!'
12-TET Tuning
12
!
100.00000
200.00000
300.00000
400.00000
500.00000
600.00000
700.00000
800.00000
900.00000
1000.00000
1100.00000
2/1
```

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## 3.5.3 Fluidsynth

```
pytuning_tuning_tables.create_fluidsynth_tuning(scale, reference_note=60, chan=[0], bank=0, prog=[0])
```

Create a Fluidsynth tuning table

#### **Parameters**

- scale The scale to model (list of frequency ratios)
- reference\_note The MIDI number of the absolute frequency reference
- chan A list of channels for which to create the table
- bank The bank for the tuning table
- prog A list of program numbers for the tuning table

**Returns** A Fluidsynth tuning table as a String

The default value of reference\_note pegs the scale to to the standard concert tuning of middle C (A = 440Hz).

The Fluidsyny tuning model allows each channel, bank, and program to have a different tuning. Thus, if one, say, wants all programs to be tuned to the scale, the tuning table can get quite large.

As a somewhat detailed example, let's say that the user had a 12-EDO scale constructed, and wanted to pin the tonic note to the standard A440. The following will do this:

```
from pytuning.scales import create_edo_scale
from pytuning.tuning_tables import create_timidity_tuning

scale = create_edo_scale(12)
tuning_table = create_fluidsynth_tuning(scale, prog=range(128), reference_note=69)
```

with the first part of the table given by:

```
# Fluidsynth Tuning Table created by pytuning

# Note reference: 69; Freq reference: 440.000000 Hz

tuning tuning000 0 0

tune 0 0 0 0.000000

tune 0 0 1 100.000000

tune 0 0 2 200.000000

tune 0 0 3 300.000000

tune 0 0 4 400.000000

tune 0 0 5 500.000000

tune 0 0 6 600.000000

tune 0 0 7 700.000000

tune 0 0 8 800.000000

tune 0 0 9 900.000000

tune 0 0 9 900.000000
```

To use the table, one should start fluidsynth with the **-f** option:

```
fluidsynth -f table.name
```

#### 3.5.4 **Csound**

For use in Csound PyTuning will generate a table of frequencies that can be used as a table lookup, mapped to MIDI note number. As mentioned in the basic concepts, the easiest way to use this is via the table opcode:

```
inote init p4
iveloc init p5
ifreq table inote, 1
al oscil iveloc, ifreq, 2
outs al, al
```

#### **Parameters**

- scale The scale (list of frequency ratios)
- reference\_note The MIDI number of the absolute frequency reference
- table\_num The f table number to use

CSound has many ways of generating microtonalities. For pytuning a table lookup keyed on MIDI note number is used.

As an example of use, let's say that we want to use the 12-EDO scale with the tonic at A440:

```
from pytuning.scales import create_edo_scale
from pytuning.tuning_tables import create_timidity_tuning

scale = create_edo_scale(12)
table = create_csound_tuning(scale, reference_note=69)
```

This will produce the following output, which can be included in the CSound score file:

f1 0 256	-2 8.17580 8.66196	9.17702	9.72272	10.30086	10.
<b>→</b> 91338	11.56233 12.24986 \				
	12.97827 13.75000	14.56762	15.43385	16.35160	17.
<b>→</b> 32391	18.35405 19.44544 \				
	20.60172 21.82676	23.12465	24.49971	25.95654	27.
<b>→</b> 50000	29.13524 30.86771 \				
	32.70320 34.64783	36.70810	38.89087	41.20344	43.
<b>⇔</b> 65353	46.24930 48.99943 \				
	51.91309 55.00000	58.27047	61.73541	65.40639	69.
<b>→</b> 29566	73.41619 77.78175 \				
	82.40689 87.30706	92.49861	97.99886	103.82617	110.
<b>→</b> 00000	116.54094 123.47083 \				
	130.81278 138.59132	146.83238	155.56349	164.81378	174.
<b>→</b> 61412	184.99721 195.99772 \				
	207.65235 220.00000	233.08188	246.94165	261.62557	277.
<b>→</b> 18263	293.66477 311.12698 \				
	329.62756 349.22823	369.99442	391.99544	415.30470	440.
<b>→</b> 00000					
	523.25113 554.36526	587.32954	622.25397	659.25511	698.
<b>→</b> 45646	739.98885 783.99087 \				
	830.60940 880.00000	932.32752	987.76660	1046.50226	1108.
<b>→</b> 73052	1174.65907 1244.50793 \				
	1318.51023 1396.91293	1479.97769	1567.98174	1661.21879	1760.
<b>→</b> 00000	1864.65505 1975.53321 \				
	2093.00452 2217.46105	2349.31814	2489.01587	2637.02046	2793.
→82585	2959.95538 3135.96349 \				
	3322.43758 3520.00000	3729.31009	3951.06641	4186.00904	4434.
→92210	4698.63629 4978.03174 \				
	5274.04091 5587.65170	5919.91076	6271.92698	6644.87516	7040.
→00000	7458.62018 7902.13282 \				

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```
8372.01809 8869.84419 9397.27257 9956.06348 10548.08182 11175.
→30341 11839.82153 12543.85395
```

# 3.6 Number Theory

While this part of the package isn't particularly fleshed out yet, there are a few number-theoretic functions for the analysis of scales.

#### 3.6.1 Odd Limits

PyTuning contains functions for finding the odd Limit for both intervals and scales.

We can define and interval – say,  $\frac{45}{32}$ , and find its odd-limit with the following:

```
from pytuning.number_theory import odd_limit
interval = sp.Rational(45,32)
limit = odd_limit(interval)
```

which yields and answer of 45.

One can also find the odd limit of an entire scale with the find odd limit for scale () function:

```
from pytuning.scales import create_euler_fokker_scale
from pytuning.number_theory import find_odd_limit_for_scale
scale = create_euler_fokker_scale([3,5],[3,1])
limit = find_odd_limit_for_scale(scale)
```

which yields 135. (Examining the scale:

$$\left[1, \quad \frac{135}{128}, \quad \frac{9}{8}, \quad \frac{5}{4}, \quad \frac{45}{32}, \quad \frac{3}{2}, \quad \frac{27}{16}, \quad \frac{15}{8}, \quad 2\right]$$

you will see that this is the largest odd number, and is found in the second degree.)

```
pytuning.number_theory.odd_limit(i)
```

Find the odd-limit of an interval.

**Parameters i** – The interval (a sympy.Rational)

**Returns** The odd-limit for the interval.

```
pytuning.number_theory.find_odd_limit_for_scale(s)
```

Find the odd-limit of an interval.

**Parameters** s – The scale (a list of sympy.Rational values)

**Returns** The odd-limit for the scale.

## 3.6.2 Prime Limits

One can also compute prime limits for both scales and intervals. Extending the above example, one would assume that the Euler-Fokker scale would have a prime-limit of 5, since that's the highest prime used in the generation, and in fact:

```
from pytuning.scales import create_euler_fokker_scale
from pytuning.number_theory import find_prime_limit_for_scale

scale = create_euler_fokker_scale([3,5],[3,1])
limit = find_prime_limit_for_scale(scale)
```

will return 5 as the limit.

```
pytuning.number_theory.prime_limit(i) Find the prime-limit of an interval.
```

**Parameters i** – The interval (a sympy.Rational)

**Returns** The prime-limit for the interval.

```
pytuning.number_theory.find_prime_limit_for_scale(s) Find the prime-limit of an interval.
```

**Parameters** s – The scale (a list of sympy.Rational values)

**Returns** The prime-limit for the scale.

# 3.7 Utilities

The PyTuning package contains some utilities which may be useful. In general these tend to be smaller utilities and tasks that are useful in the analysis of musical scales, but they are not full-featured "things" in and of themselves.

#### 3.7.1 Interval Normalization

```
pytuning.utilities.normalize_interval(interval, octave=2)
    Normalize a musical interval
```

#### Parameters

- **interval** The interval to normalize. Should be a frequency ratio, most usefully expressed as a *sympy.Rational* or related data item
- octave The formal octave. Defaults to 2

**Returns** The interval, normalized

Note that any formal octave can be used. In normal usage a 2 will be used (i.e., a doubling of frequency is an octave).

Normalization works by finding the smallest power of two (or octave) that when multiplied by the interval (in the case of an interval less than 1) or divided into the interval (for intervals greater than 2) will bring the interval into the target range of  $1 \le i \le 2$ .

As an example, the interval 9 would normalize to  $\frac{9}{8}$ , because 9 needs to be scaled down by three octaves to fall within the limit of 1 and 2:

$$\frac{9}{8} = \frac{9}{2^3}$$

```
ni = normalize_interval(sp.Integer(9))
print(ni)
9/8
```

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One can also normalize on a non-standard interval, for example, 3:

```
ni = normalize_interval(sp.Integer(34), octave=3)
print(ni)
34/27
```

### 3.7.2 Distinct Intervals

pytuning.utilities.distinct\_intervals(scale)

Find the distinct intervals in a scale, including inversions

**Parameters** scale – The scale to analyze

**Returns** A list of distinct intervals

The scale should be specified as a list of sympy numerical values (Rational or Integer). Note that the convention adopted in this code is that scale[0] is a unison and scale[-1] is the formal octave (often 2).

As an example of a valid scale, a standardized Pythagorean tuning could be passed into the function:

$$\left[1, \frac{256}{243}, \frac{9}{8}, \frac{32}{27}, \frac{81}{64}, \frac{4}{3}, \frac{1024}{729}, \frac{3}{2}, \frac{128}{81}, \frac{27}{16}, \frac{16}{9}, \frac{243}{128}, 2\right]$$

If one were hand-crafting this scale, it would look something like:

```
import sympy as sp
scale = [sp.Integer(1), sp.Rational(256,243), sp.Rational(9,8), ...]
```

The function returns a list in rational/symbolic terms. If numerical values are needed, one can, for example, map ratio\_to\_cents to obtain it:

```
di = distinct_intervals(scale)
di_in_cents = [ratio_to_cents(x) for x in di]
```

distinct\_intervals() returns all the distinct intervals within a musical scale. Note, though, that it does not include the unison (or the octave) in the results, as all scales contain those intervals by definitions.

As an example, if we were to take a Pythagorean scale and find the intervals that exist within it:

```
pythag = create_pythagorean_scale()
di = distinct_intervals(pythag)
```

we end up with:

```
2187
        256
               8192
                       262144
                                 4096
                                             243
                                                    1024
                                                            19683
                                                                     729
                                                                            6561
                                                                                    65536
                                                                                             177147
                                                                                                       59049
                                                                                                                81
        \overline{243}
              6561
                      177147
                                2187'
                                             128
                                                     729
                                                                                                                64
2048
                                                            16384
                                                                     512
                                                                            4096
                                                                                    59049
                                                                                             131072
                                                                                                       32768
```

# 3.7.3 Converting a Ratio to a Cent Value

```
pytuning.utilities.ratio_to_cents(ratio)
```

Convert a scale degree to a cent value

**Parameters ratio** – The scale degree (sympy value)

**Returns** The scale degree in cents

Calculates:

$$\sqrt[2]{\frac{1}{1200}}\sqrt{\text{degree}}$$

Note that this function returns a floating point number, not a sympy ratio.

This function is useful if you have a symbolic value (a rational or transcendental, for example) and you want to see its value in cents (a logarithmic scale in which there are 1200 steps in a factor of two). For example:

```
interval = sp.Rational(3,2) # A perfect fifth
cents = ratio_to_cents(interval)
print(cents)
701.955000865387
```

# 3.7.4 Converting a Cent Value to a Ratio

```
pytuning.utilities.cents_to_ratio (cents)
Convert a cent value to a ratio
```

Parameters cents - The degree value in cents

**Returns** the frequency ratio

This function takes a cent value and returns it as a frequency ratio (a sympy floating point number).

```
print(cents_to_ratio(700.0))
1.49830707687668
```

(In other words, the 12-EDO fifth (700 cents) is very close to that of the Pythagorean fifth  $(\frac{3}{2}, \text{ or } 1.5)$ .)

# 3.7.5 Converting a Note Number to a Frequency

```
pytuning.utilities.note_number_to_freq(note, scale=None, reference_note=69, reference_frequency=440.0)

Convert a note number (MIDI) to a frequency (Hz).
```

#### **Parameters**

- **note** (reference) The note number (0<=note<=127)
- scale The scale. If none it assume EDO 12.
- note The conversions reference note
- reference\_frequency The frequency of the reference note

**Returns** The frequency of the note in Hertz

The default values for reference\_note and reference\_frequency correspond to standard orchestral tuning, a4 = 440 Hz.

With this function we can calculate the frequency of any note number. If defaults to the MIDI standard, which pegs note number 69 to 440 Hz and uses a 12-EDO scale.

As an example, MIDI note 60 (Middle-C):

```
print (note_number_to_freq(60))
261.625565300599
```

But if, for example, we wanted to use a different pitch standard, we could peg A to 444 Hz.

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```
print(note_number_to_freq(60, reference_frequency=444.0))
264.003979530604
```

You can also pass in a non-EDO tuning if you're converting a different kind of scale to frequencies. This is used often in the code associated with the tuning tables.

# 3.7.6 Naming A Ratio

```
pytuning.utilities.ratio_to_name (ratio)
Convert a scale degree to a name

Parameters ratio - The input scale degree (a sympy value)
```

Returns The degree name if found, None otherwise

This function will look up the name of a ratio and return it (returning None) if it is not found.

As an example:

```
pythag = create_pythagorean_scale()
names = [ratio_to_name(x) for x in pythag]
```

names now contains:

```
['Unison',
'Pythagorean Minor Second',
'Pythagorean Major Second',
'Pythagorean Minor Third',
'Pythagorean Major Third',
'Perfect Fourth',
'Pythagorean Diminished Fifth',
'Perfect Fifth',
'Pythagorean Minor Sixth',
'Pythagorean Major Sixth',
'Pythagorean Minor Seventh',
'Pythagorean Major Seventh',
'Octave']
```

There are currently about 260 intervals in the internal catalog, so while not complete, the database is fairly extensive.

# 3.7.7 Comparing Two Scales

```
pytuning.utilities.compare_two_scales (scale1, scale2, reference_freq=220.0, title=['Scale1', 'Scale2'])

Compare two scales

param scale1 The first scale (list of sympy values)

param scale2 The second scale (list of sympy values)

param reference_freq The frequency (Hz) of the first degree

param title The scale names (list of strings with len = 2)

returns None, (ie nothing)
```

This function will produce a simple textual representation of the difference between two scales. As an example, comparing the 12-EDO and Pythagorean scales:

```
from pytuning.scales import create_edo_scale, create_pythagorean_scale
from pytuning.utilities import compare_two_scales

scale_1 = create_edo_scale(12)
scale_2 = create_pythagorean_scale()

compare_two_scales(scale_1, scale_2, title=['12-TET', 'Pythagorean'])
```

#### produces:

12-TET		Pythagorean		
Cents	Freq	Cents	Freq	Delta(Cents)
0.0000	220.0000	0.0000	220.0000	0.0000
100.0000	233.0819	90.2250	231.7695	9.7750
200.0000	246.9417	203.9100	247.5000	-3.9100
300.0000	261.6256	294.1350	260.7407	5.8650
400.0000	277.1826	407.8200	278.4375	-7.8200
500.0000	293.6648	498.0450	293.3333	1.9550
600.0000	311.1270	588.2700	309.0261	11.7300
700.0000	329.6276	701.9550	330.0000	-1.9550
800.0000	349.2282	792.1800	347.6543	7.8200
900.0000	369.9944	905.8650	371.2500	-5.8650
1000.0000	391.9954	996.0900	391.1111	3.9100
1100.0000	415.3047	1109.7750	417.6562	-9.7750
1200.0000	440.0000	1200.0000	440.0000	0.0000

# 3.8 Visualizations

PyTuning includes some visualizations for the analysis of scales, but this is not yet fleshed out.

The graphics are via Matplotlib, which is the *de facto* implementation of analytical graphics for python. There is also an optional dependency on Seaborn. Seaborn is good to include if you can – it makes the graphs better – but it's a large package, owning to its dependencies (which include SciPy and Pandas; great packages, but extensive and large). If you have disk space to spare you may want to install it; otherwise you can get my with Matplotlib alone. On my system SciPy and Pandas weigh in at about 200 megabytes, not including any dependencies that *they* require. Matplotlib, on the other hand, is about 26 megabytes.

#### 3.8.1 The Consonance Matrix

It's nice to be able to get an intuitive feeling for the consonance or dissonance of a scale. For this, the **consonance** matrix is provided.

The consonance matrix forms an interval between every degree in the scale and applies a metric function to it. The default metric function just measures the denominator of the interval after any simplification it can undergo (and is really only meaningful for degrees which are expressed an integer ratios).

As an example, we can create a scale of the Euler-Fokker type:

```
scale = create_euler_fokker_scale([3,5],[2,1])
```

which is

$$\left[1, \quad \frac{9}{8}, \quad \frac{5}{4}, \quad \frac{45}{32}, \quad \frac{3}{2}, \quad \frac{15}{8}, \quad 2\right]$$

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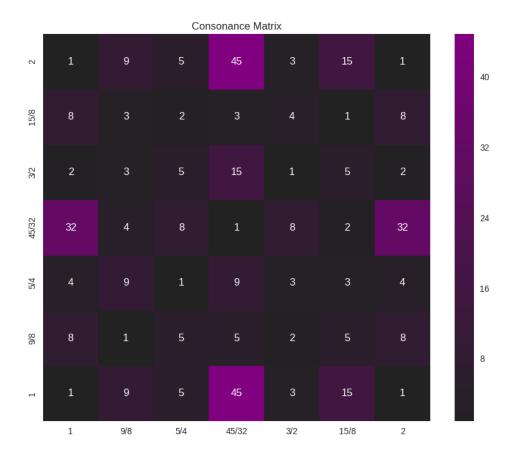
Now, to create a consonance matrix:

```
from pytuning.visualizations import consonance_matrix
matrix = consonance_matrix(scale)
```

matrix now contains a matplotlib Figure. To write it as PNG:

```
matrix.savefig('consonance.png')
```

Which yields:



Because this function accepts an arbitrary metric, it can be used for any analysis performed on the intervals of a scale; it does not need to really be a measurement or estimate of consonance. As an example, let's say that (for some reason) you're interested in how far from unity each interval is:

```
def metric_unity(degree):
    normalized_degree = normalize_interval(degree)
    y = abs (1.0 - normalized_degree.evalf())
    return y

scale = create_euler_fokker_scale([3,5],[2,1])
matrix = consonance_matrix(scale, metric_function=metric_unity, title="Distance from_ounity")
```

Our graph now looks like:



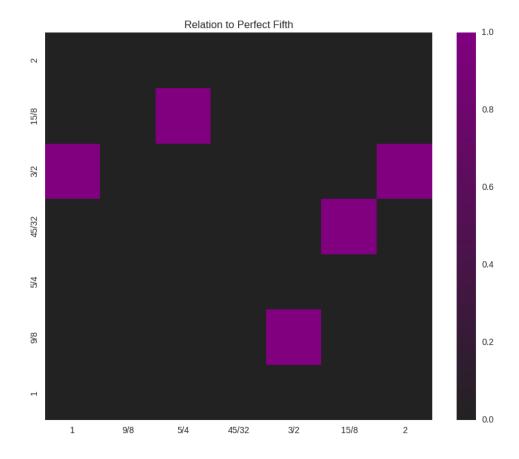
We could even do something like look for perfect fifths within our scale:

```
def metric_fifth(degree):
    p5 = sp.Rational(3,2)
    normalized_degree = normalize_interval(degree)
    y = normalize_interval(p5 / normalized_degree).evalf()
    y = y if y == 1 else 0
    return y

scale = create_euler_fokker_scale([3,5],[2,1])
matrix = consonance_matrix(scale, metric_function=metric_fifth,
    title="Relation to Perfect Fifth", annot=False)
```

which gives us:

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where the highlighted cells denote perfect fifths.

You'll note that the entry for  $\frac{45}{32}$  and  $\frac{15}{8}$  is 1 (a perfect fifth). We can verify this:

```
print(normalize_interval(sp.Rational(45,32) / sp.Rational(15,8)))
3/2
```

```
pytuning.visualizations.consonance_matrix(scale, metric\_function=None, figsize=(10, 8), title='Consonance Matrix', annot=True, cmap=None, fig=None, vmin=None, vmax=None)
```

Display a consonance matrix for a scale

#### **Parameters**

40

- scale The scale to analyze (list of frequency ratios)
- metric\_function The metric function (see below)
- figsize Size of the figure (tuple, in inches)
- title the graph title
- annot If *True*, display the value of the metric in the grid cell
- cmap A custom matplotlib colormap, if desired

- fig a matplotlib.figure.Figure or None. If None a figure will be created
- vmin If secified, the lowest value of the range to plot. Only works if Seaborn is included.
- vman If secified, the largest value of the range to plot. Only works if Seaborn is included.

Returns a matplotlib. Figure for display

The consonance matrix is created by taking each scale degree along the bottom and left edges of a matrix, forming a frequency ratio between the left and bottom value, and applying the metric function to that value.

The default metric function is the denominator of the normalized ratio – the thought being that the smaller this number is the more consonant the interval.

If a user-specified metric function is used, that function should accept one parameter (the ratio) and return one value. As an example, the default metric function:

```
def metric_denom(degree):
   normalized_degree = normalize_interval(degree)
   return sympy.fraction(normalized_degree)[1]
```

Note that, as with most parts of this code, the ratios should be expressed in terms of sympy values, usually sympy.Rational's

A note of figures: With the default of fig=None, this function will just produce a figure and return it for display. However, if one wants to plot multiple figures and can pre-allocate it. This is useful, for example, if one wants to plot multiple figures on the same chart. As an example, the following will plot two separate consonance matrices, side-by-side:

```
import matplotlib.pyplot as plt
fig = plt.figure(figsize=(15,6))
plt.subplot(plt.GridSpec(1, 2)[0,0])
fig = consonance_matrix(scale,title="Full Scale", fig=fig)
plt.subplot(plt.GridSpec(1, 2)[0,1])
fig = consonance_matrix(mode_scale,title="Mode Scale", fig=fig)
fig
```

vmin and vmax are useful if you're plotting multiple graphs in the same figure; they can be used to ensure that all the component graphs use the same scale, so that visually the graphs are related. Otherwise each graph will have its own scale.

# 3.9 Using PyTuning Interactively

With a little knowledge of Python, one can use PyTuning in an interactive environment.

If you plan on doing this, I recommend using the Jupyter QtConsole. Jupyter is a full-featured interactive environment for several programming languages (the project started as IPython, but has expanded to cover many languages).

Included in the distribution is a script, interactive.py, which is useful for setting up your environment.

# 3.9.1 Installing Jupyter

(Note: I have experience with Linux and MacOS, so these instructions are focused on these platforms. Jupyter runs under Windows, but I have no experience on that platform.)

On Linux, good ways of installing Jupyter include using your native package manager or installing it via a third-party distribution.

#### **Native Packages**

On Ubuntu Jupyter is still referred to as IPython. On Xenial, for example, there are packages for both Python 2.7 and Python 3:

#### On Arch Linux:

```
mark@lucid:~$ pacman -Ss qtconsole community/python-qtconsole 4.2.1-1 Qt-based console for Jupyter with support for rich media output community/python2-qtconsole 4.2.1-1 Qt-based console for Jupyter with support for rich media output mark@lucid:~$
```

(PyTuning will run under either Python 2.7 or Python 3.X, so the version you install is up to you.)

I would also suggest installing Matplotlib so that graphics can be used within the console, i.e:

```
vagrant@ubuntu-xenial:~$ aptitude search matplotlib
p python-matplotlib
                                            - Python based plotting system in a
⇒style similar to
  python-matplotlib:i386
                                            - Python based plotting system in a...
→style similar to
p python-matplotlib-data
                                            - Python based plotting system (data_
→package)
  python-matplotlib-dbg
                                            - Python based plotting system (debug_
→extension)
  python-matplotlib-dbg:i386
                                            - Python based plotting system (debug
→extension)
  python-matplotlib-doc
                                            - Python based plotting system.
\hookrightarrow (documentation packag
  python-matplotlib-venn
                                            - Python plotting area-proportional two-_
→and three-w
  python3-matplotlib
                                            - Python based plotting system in a_
⇒style similar to
p python3-matplotlib:i386
                                            - Python based plotting system in a_
⇒style similar to
p python3-matplotlib-dbg
                                            - Python based plotting system (debug
→extension, Pyt
p python3-matplotlib-dbg:i386
                                            - Python based plotting system (debug_
⇔extension, Pyt
                                            - Python 3 plotting area-proportional.
  python3-matplotlib-venn
→two- and three
vagrant@ubuntu-xenial:~$
```

#### And optionally Seaborn:

```
vagrant@ubuntu-xenial:~$ aptitude search seaborn
p python-seaborn - statistical visualization library
p python3-seaborn - statistical visualization library
vagrant@ubuntu-xenial:~$
```

(But note that Seaborn is a bit large. See the discussion in Visualizations.)

## **Third Party Packages**

Jupyter can also be installed via third-party Python distributions. This is my preferred way of doing it, and on MacOS it is (in my opinion) the only viable option. I imagine that a third-party distribution would be the easiest way to do this on Windows.

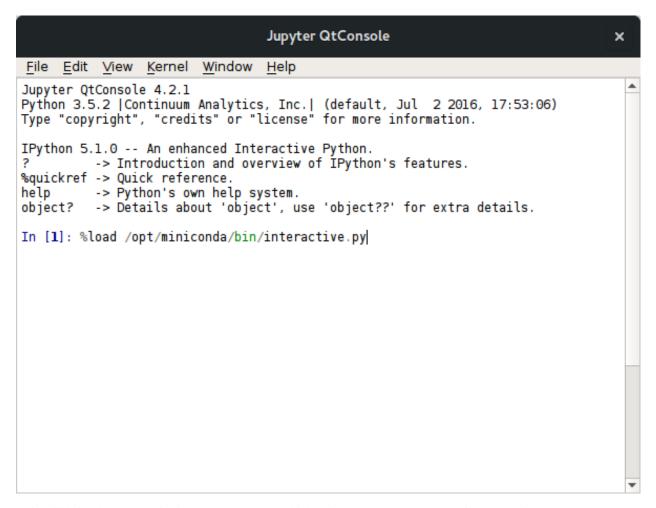
One good distribution is Continuum Analytics Miniconda. Once miniconda is installed, the conda tool can be used to install the necessary packages:

vagrant@ubuntu-xenial:~\$ conda install jupyter qtconsole matplotlib seaborn sympy\_ →numpy

# 3.9.2 Setting the Environment

The PyTuning distribution contains a script, interactive.py, that can be used to import the package into your namespace, as well as setting up some convenience functions. Where that script lives on your computer can vary by platform as well as python distribution. If you're on Linux and installed PyTuning with your system python, there's a good chance it's in /usr/bin. If you installed into the Miniconda distribution, then it will probably be somewhere like ~/miniconda/bin.

Once you've launched the console, this script should be loaded into the environment with the %load command. This will load it into the console, but you'll need to execute it. This is normally done with Shitf-enter, although Control-enter may be used on some platforms/versions.



This will bring load the script into the console, at which point a [Shit-Enter] will execute it.

```
Jupyter QtConsole
                                                                                   ×
          View Kernel Window
File
    Edit
                                 Help
  ...: def euler fokker():
           global scale
  . . . :
           global cents
  . . . :
           intervals = input("Intervals (list of prime integers): ")
                           = input("Formal Octave (2):")
           if len(octave) == 0:
               octave = 2
           else:
               octave = int(octave)
           exec("int parsed =%s" % intervals, globals())
           multiplicities = [1]* len(intervals)
           scale = create_euler_fokker_scale(int_parsed, multiplicities, octave)
           print( "Current Scale:")
           display(scale)
           cents = [ratio_to_cents(x) for x in scale]
  ...: def set generators():
           global generators
  . . . :
           index = 0
           for entry in all constructors:
               print( index, entry[1])
               index = index + 1
           selected = input("Which generator?:")
           generators = all_constructors[int(selected)][0]
  ...: Interval = lambda p, q: normalize interval(sp.Rational(p,q))
```

# 3.9.3 A (Very) Brief Introduction to Jupyter

There are a few things about Jupyter which are useful for interacting with the Python interpreter.

#### **Tab Completion**

Jupyter has a very good tab completion system which can save a lot of typing.

As a first example, the %load command (above) can use completion to navigate to the file. One need only type enough to disambiguate each directory in the path and the tab will complete it, much in the same way that the bash shell will do so.

Tab completion can also be used to find functions that are defined in your namespace. As an example, by typing create\_ into the console and hitting tab you will see all objects and functions that begin with that string, and by hitting the tab a second time a selector will be brought up that allows you to select the function you're after:



### **Tool Tips**

Jupyter also has a nice tool-tip function that will show a function's documentation once the opening ( is typed:

```
Jupyter QtConsole
File Edit View Kernel Window
In [3]: create_harmonic_scale(
                                 Signature: create_harmonic_scale(first_harmonic, last_harmonic, normalize=True,
                                 octave=2)
                                Docstring:
                                 Create a harmonic scale
                                 param first_harmonic: The first harmonic:
                                 :param last harmonic: The last harmonic
:param normalize: If true, normalize the scale to an octave
                                                    (2/1 by default, otherwise taken from
                                 :param octave: The definition of the formal octave.
                                 :returns: The scale
                                 As an example of use, a normalized scale constructed from harmonics
                                 3 to 20:
                                 .. code::
                                     scale = create_harmonic_scale(3,20)
                                 which yields:
                                 [Documentation continues...]
```

#### **History**

Jupyter also has a nice history function. If, for example, at some point in your session you entered the following:

```
In [3]: scale = create_harmonic_scale(2,6)
In [4]:
```

Then, later on in the session if you type scale =, each time you hit the up arrow it will search through your history and bring up lines beginning with that character string. You can then edit that line and make changes.

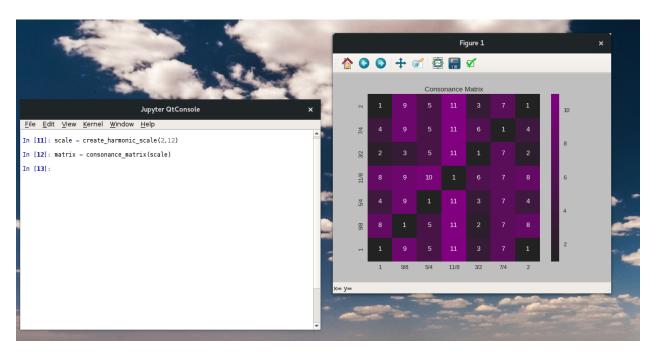
```
In [3]: scale = create_harmonic_scale(2,6)
In [4]: scale2 = create_harmonic_scale(2,7)
In [5]:
```

#### **Rich Display**

By default scales and degrees will be displayed symbolically. If you want text display you can use the print() function.

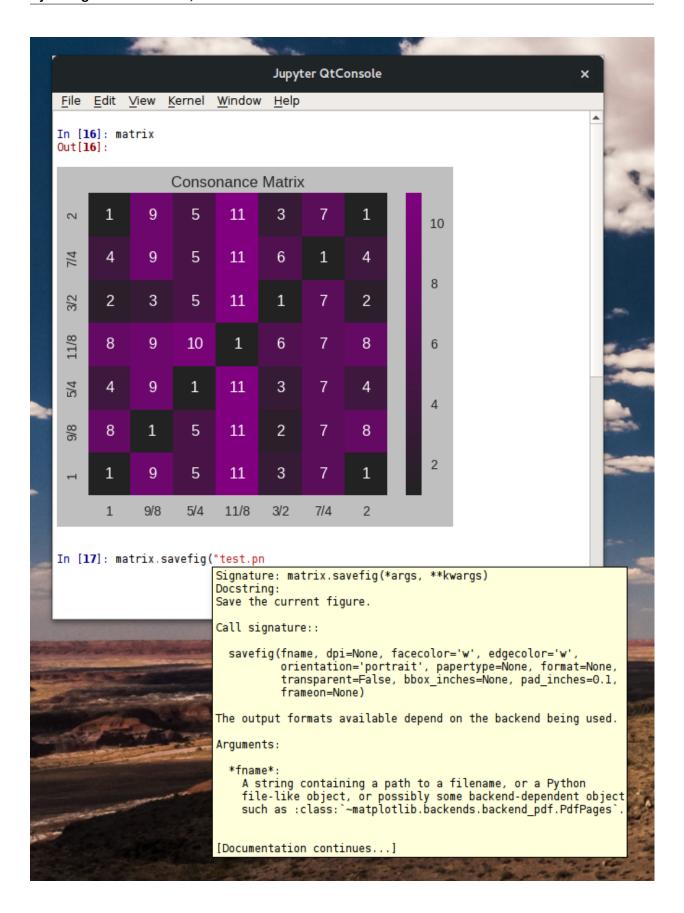
#### **Graphics**

With matplotlib installed one also has access to graphics. A graph can be displayed within the console, or it can be displayed in a simple viewer that allows some editing and the saving of the graphic file in a few different formats (JPEG, PNG, SVG). The viewer comes up automatically. If you close it at want to bring it back up later, you can use the show() function (i.e., matrix.show()).



Note that by re-sizing the window, you re-size the graphic.

You can also save the figure directly from the console:



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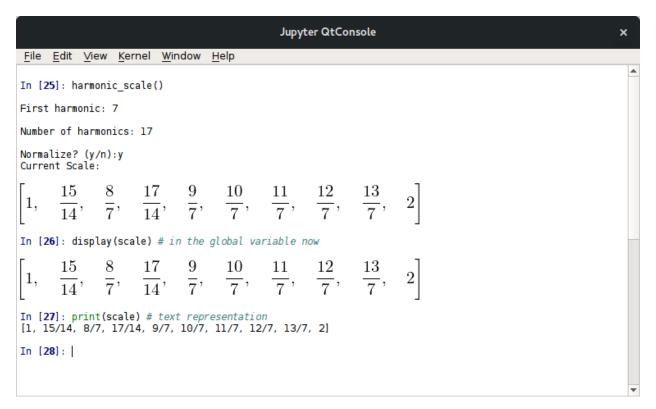
# 3.9.4 A Sample Session

On my personal website I discuss a scale that I've been working with recently for music composition. It's a mode of the harmonic scale which minimizes dissonance by one of the metrics included in the distribution. In the following session I create the scale and create two tuning tables (a timidity and scala table) for use in music composition.

### 3.9.5 Helper Functions

interactive.py also creates a few helper functions for the creation of scales. They wrap the base functions in an interactive prompt and define a global variable, scales into which the calculated scale is placed.

As an example, to create a harmonic scale:



Only a few functions have yet been written, but more will be included in future releases.

```
pytuning.interactive.harmonic_scale()
```

Create a harmonic scale in an interactive environment.

This function will prompt for the first and last harmonic, as well as the user's desire for normalization. It assumes the standard octave of 2.

The output is put into the global scale.

```
pytuning.interactive.edo_scale()
```

Create an EDO scale in an interactive environment.

This function will prompt for the number of divisions (tones) and the formal octave.

The output is put into the global scale.

```
pytuning.interactive.euler_fokker()
```

Create a scale of the Euler Fokker Genus in an interactive environment.

This function will prompt for generator primes and the formal octave. Note that multiplicities is not prompted for, so if there are repetitions they will need to be spelled out separately.

The output is put into the global scale.

# 3.9.6 Running in a Persistant Way

Jupyter also offers an interactive notebook, similar to a Matlab notebook. For more complicated analysis it is my preferred way of interacting with the PyTuning library. Documentation, graphics, equations, code, and output calculations can all be included. It can be installed in a way that is similar to the console (and in fact may be installed along with it, depending on how the packages maintainers on your platform have chosen to break things up).

The Github repository for this project has a directory which contains a rendered notebook that shows an exploration of pentatonic scales in the Pythagorean tuning. Github renders notebooks well, so you can see what's possible to

decide if you want to install the software. If you're going to be doing anything really complicated in an interactive environment, I would recommend installing and using this.

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